Solutions to Past Paper Questions – Area and Volume of Similar Shapes

- 24) Ratio of lengths = 4:8 = 1:2
 - (a) So ratio of areas = $1^2:2^2 = 1:4$ Surface area of B = $80 \times 4 = 320$ cm²
 - (b) Ratio of volumes = $1^3:2^3 = 1:8$ Volume of A = $600 \div 8 = 75 \text{cm}^3$
- 20) Ratio of Surface areas = 24:96 = 1:4
 - (a) Ratio of lengths = $\sqrt{1}$: $\sqrt{4}$ =1:2 Height of cone Q = 4 × 2 = 8cm
 - (b) Ratio of volumes = 1^3 : 2^3 = 1:8 Volume of cone Q = $12 \times 8 = 96$ cm³
- 16) Ratio of lengths = 4:6 = 2:3

So ratio of volumes = $2^3:3^3 = 8:27$ Volume of cylinder B = $80 \times \frac{27}{8} = 270 \text{ cm}^3$

21) Ratio of volumes = 27:125So ratio of lengths = $\sqrt[3]{27}:\sqrt[3]{125}=3:5$ So ratio of areas = $3^2:5^2 = 9:25$

Surface area of larger solid = $36 \times \frac{25}{9} = 100 \text{ cm}^2$

- 12) Ratio of lengths = 20:30 = 2:3Ratio of areas = $2^2:3^2 = 4:9$ Surface area of larger frustum = $450 \times \frac{9}{4} = 1012.5 \text{ cm}^2$
- 23) Ratio of volumes = 12000:49152 = 125:512Ratio of lengths = $\sqrt[3]{125}:\sqrt[3]{512}=5:8$ Ratio of areas = $5^2 8^2 = 25:64$

Surface area of larger prism = $9728 \times \frac{25}{64} = 3800 \text{ cm}^2$