

Solutions to Past Paper Questions – Angles in Circles

13) (a) (i) $\text{RPQ} = 56^\circ$ (alternate segment theorem)

(ii) $\text{ROQ} = 112^\circ$ (angle at centre is twice angle at circumference)

(b) (i) $\text{BAD} = 180 - 132 = 48^\circ$ (opposite angles of cyclic quadrilateral)

So $\text{BAC} = 48 - 25 = 23^\circ$

(ii) $\text{ABC} = 90^\circ$ (angle in a semicircle)

$\text{DBC} = 25^\circ$ (angles in the same segment)

So $\text{ABD} = 90 - 25 = 65^\circ$

10) (a) $\text{PQR} = 90^\circ$ (angle in a semicircle)

(b) $\text{PRQ} = 56^\circ$ (angles in the same segment)

(c) $\text{POQ} = 112^\circ$ (angle at centre is twice angle at circumference)

12) (a) $\text{BAC} = 80^\circ \div 2 = 40^\circ$ (angle at centre is twice angle at circumference)

(b) $\text{OBC} = (180^\circ - 80^\circ) \div 2 = 50^\circ$ (OBC is an isosceles triangle)

$\text{ABC} = 38^\circ$ (alternate segment theorem)

So $\text{OBA} = 50^\circ - 38^\circ = 12^\circ$

(c) If we could draw a circle with diameter ED, passing through A, then EAD would be an angle in a semicircle and so would be 90° . But $\text{EAD} = 40^\circ + 38^\circ = 78^\circ$. So it is not possible.

12) (a) $\text{PQT} = 90^\circ$ (angle between tangent and radius)

so $\text{PQR} = 90^\circ - 56^\circ = 34^\circ$

(b) $\text{PRQ} = 90^\circ$ (angle in a semicircle)

$\text{QRT} = 56^\circ$ (TR = TQ because both are tangents, so TRQ is isosceles)

$\text{PRT} = 90^\circ + 56^\circ = 146^\circ$