

Converting recurring decimals to fractions

1) Change each of the following decimals to a fraction in lowest terms:

- (a) 0.36 (b) 0.363636... (c) 0.5363636... (d) 0.3666... (e) 0.555...
- (f) 0.012 (g) 0.012012... (h) 0.0121212... (i) 0.01222... (j) 0.055...

Solutions

1) (a) $\frac{36}{100} = \frac{9}{25}$

(b) $x = 0.36363636\dots$
 $100x = 36.363636\dots$

Subtract: $99x = 36$
 $x = \frac{36}{99} = \frac{4}{11}$

(c) $x = 0.536363636\dots$
 $100x = 53.6363636\dots$

Subtract: $99x = 53.1$
 $x = \frac{53.1}{99} = \frac{531}{990} = \frac{59}{110}$

(d) $x = 0.366666\dots$
 $10x = 3.666666\dots$

Subtract: $9x = 3.3$
 $x = \frac{3.3}{9} = \frac{33}{90} = \frac{11}{30}$

(e) $x = 0.55555555\dots$
 $10x = 5.55555555\dots$

Subtract: $9x = 5$
 $x = \frac{5}{9}$

(f) $\frac{12}{1000} = \frac{3}{250}$

(g) $x = 0.012012012012\dots$
 $1000x = 12.012012012\dots$

Subtract: $999x = 12$
 $x = \frac{12}{999} = \frac{4}{333}$

(h) $x = 0.012121212\dots$
 $100x = 1.212121212\dots$

Subtract: $99x = 1.2$
 $x = \frac{1.2}{99} = \frac{12}{990} = \frac{2}{165}$

(i) $x = 0.012222222\dots$
 $10x = 0.12222222\dots$

Subtract: $9x = 0.11$
 $x = \frac{0.11}{9} = \frac{11}{900}$

(j) $x = 0.05555555\dots$
 $10x = 0.55555555\dots$

Subtract: $9x = 0.5$
 $x = \frac{0.5}{9} = \frac{5}{90} = \frac{1}{18}$