

Past Paper Questions – Upper and Lower Bounds

19. To the nearest centimetre,  $x = 4$  cm and  $y = 6$  cm.

(a) Calculate the upper bound for the value of  $xy$

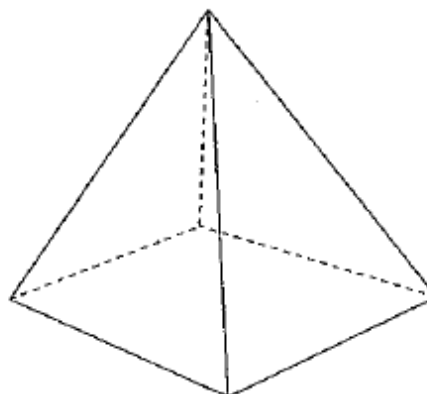
.....  
(2)

(b) Calculate the lower bound for the value of  $\frac{x}{y}$

Give your answer correct to 3 significant figures.

.....  
(3)

20.



The pyramid Cheops in Egypt is a square based pyramid.

The length of a side of the square base is 230 metres.

The vertical height of the pyramid is 146 metres.

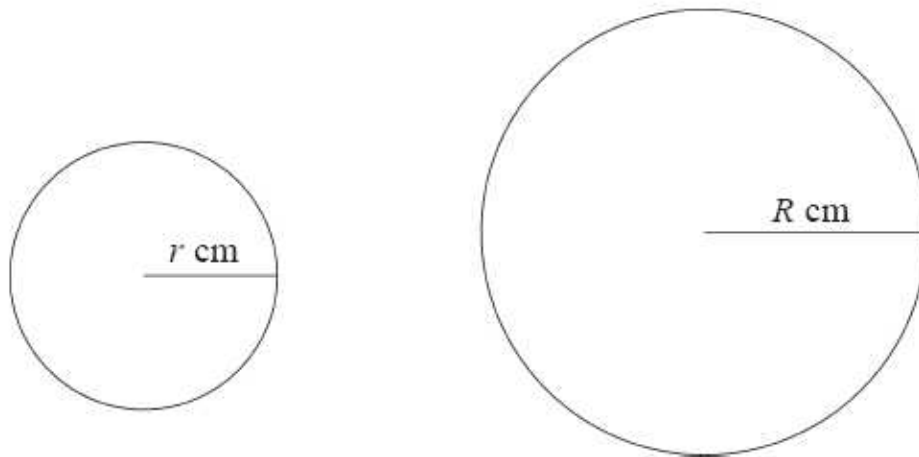
Both measurements are correct to the nearest metre.

(a) Calculate the difference between the upper bound and the lower bound of the volume of the pyramid.

Give your answer correct to 3 significant figures.

16.

Diagram **NOT**  
accurately drawn



The diagram represents two metal spheres of different sizes.

The radius of the smaller sphere is  $r$  cm.

The radius of the larger sphere is  $R$  cm.

$r = 1.7$  correct to 1 decimal place.

$R = 31.0$  correct to 3 significant figures.

(a) Write down the upper and lower bounds of  $r$  and  $R$ .

Upper bound of  $r =$  .....

Lower bound of  $r =$  .....

Upper bound of  $R =$  .....

Lower bound of  $R =$  .....

(2)

(b) Find the smallest possible value of  $R - r$ .

.....

(1)

The larger sphere of radius  $R$  cm was melted down and used to make smaller spheres of radius  $r$  cm.

(c) Calculate the smallest possible number of spheres that could be made.

.....  
(4)

19. Bill has a rectangular sheet of metal.  
The length of the rectangle is **exactly** 12.5 cm.  
The width of the rectangle is **exactly** 10 cm.

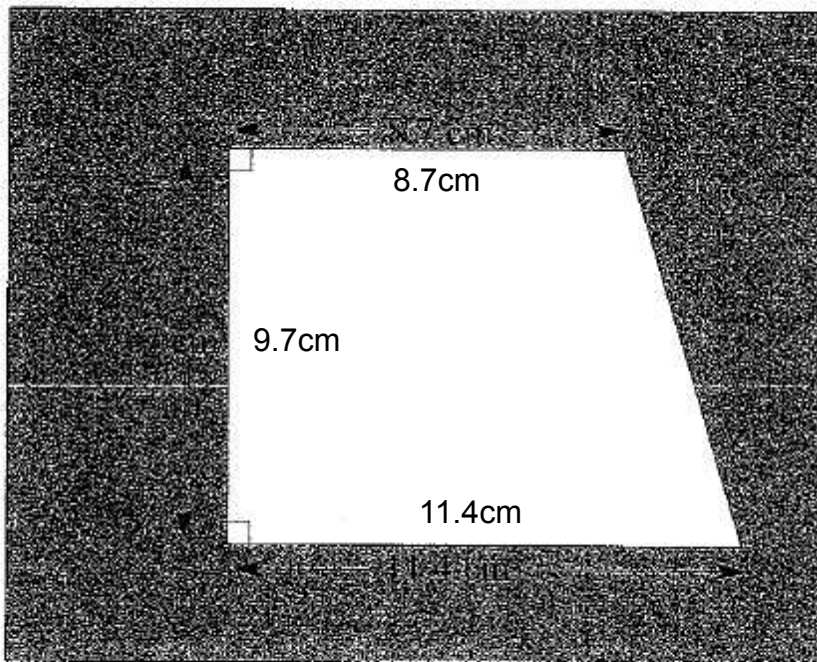


Diagram NOT accurately drawn.

Bill cuts out a trapezium.  
Its dimensions, shown in the diagram, are correct to the nearest millimetre.  
He throws away the rest of the metal sheet.

Calculate the **greatest** possible area of the rectangular sheet that he throws away.

18.

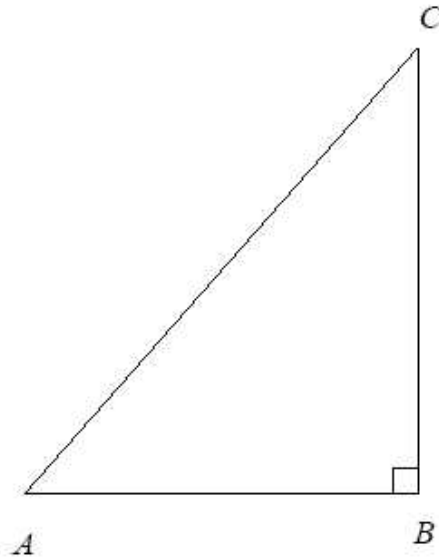


Diagram **NOT** accurately drawn

The diagram shows a triangle  $ABC$ .  
Angle  $ABC$  is **exactly**  $90^\circ$ .  
 $AB = 83$  mm correct to 2 significant figures.  
 $BC = 90$  mm correct to 1 significant figures.

(a) Calculate the upper bound for the area of triangle  $ABC$ .

.....  $\text{mm}^2$   
(2)

Angle  $CAB = x^\circ$ .

(b) Calculate the lower bound for the value of  $\tan x^\circ$ .

.....  
(2)

$ABC$  is the cross section of a triangular prism.

The upper bound for the volume of the prism is  $51561.25 \text{ mm}^3$ .  
The lower bound for the volume of the prism is  $45581.25 \text{ mm}^3$ .

(d) Write down the volume of the prism, in  $\text{cm}^3$ , to an appropriate degree of accuracy.

.....  $\text{cm}^3$   
(2)

(Total 6 marks)

9.

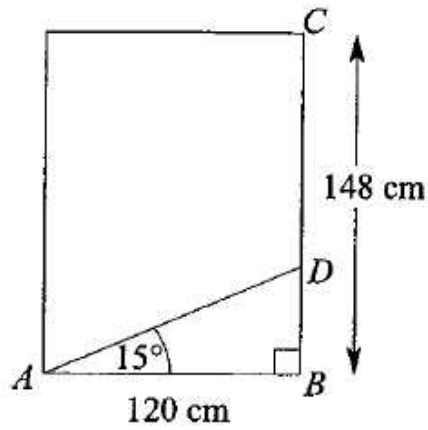


Diagram NOT accurately drawn.

$AB$  and  $BC$  are two sides of a rectangle.  
 $AB = 120$  cm and  $BC = 148$  cm.  
 $D$  is a point on  $BC$ .  
Angle  $BAD = 15^\circ$ .

- (a) Work out the length of  $CD$ .  
Give your answer correct to the nearest centimetre.

..... cm  
(4 marks)

148 is correct to 3 significant figures.  
120 is correct to 3 significant figures.  
15 is correct to the nearest whole number.

- (b) Write down the three values which should be used to work out the lower bound for the length of  $CD$ .

..... ; ..... ; .....  
(3 marks)